

# Leonidas Alaoglu Memorial Lecture

April 29th, 2025

Linde Hall 310 @ 4:30pm



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## Finite quotients of 3-manifold groups

It is well-known that for any finite group  $G$ , there exists a closed 3-manifold  $M$  with  $G$  as a quotient of the fundamental group of  $M$ . However, we can ask more detailed questions about the possible finite quotients of 3-manifold groups, e.g. for  $G$  and  $H_1, \dots, H_n$  finite groups, does there exist a 3-manifold group with  $G$  as a quotient but no  $H_i$  as a quotient? We answer all such questions. To prove non-existence, we prove new parity properties of the fundamental groups of 3-manifolds. To prove existence of 3-manifolds with certain finite quotients but not others, we use a probabilistic method, by first proving a formula for the distribution of the fundamental group of a random 3-manifold, in the sense of Dunfield-Thurston. This is joint work with Will Sawin.

**Parking:** Parking is available in Lot 3 (underground parking #126 on campus map) on California Blvd. between Wilson and Arden (near the tennis courts). Scan the QR code for a map with directions for getting to Linde Hall.



**Questions?** Please email [mathinfo@caltech.edu](mailto:mathinfo@caltech.edu) or call 626-395-4335